Exercise 46

In 2003, a town's population was 1,431. By 2007 the population had grown to 2,134. Assume the population is changing linearly.

- (a) How much did the population grow between the year 2003 and 2007?
- (b) How long did it take the population to grow from 1,431 people to 2,134 people?
- (c) What is the average population growth per year?
- (d) What was the population in the year 2000?
- (e) Find an equation for the population, P of the town t years after 2000.
- (f) Using your equation, predict the population of the town in 2014.

[TYPO: There needs to be a comma after "P" just like in the previous exercise.]

Solution

The population grew by 2134 - 1431 = 703 between 2003 and 2007, a time interval of four years. The average population growth per year is the slope,

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{2134 - 1431}{2007 - 2003} = \frac{703}{4} = 175.75.$$

In order to predict the population in 2000 and 2014, an equation of a line is needed. Let t be the number of years after 2000, and use the two points, (3, 1431) and (7, 2134). Use the point-slope formula with either of these points to get the equation of the line.

$$y - 1431 = 175.75(t - 3)$$
$$y - 1431 = 175.75t - 527.25$$
$$y = 175.75t + 903.75$$

To get the population in 2000, plug in t = 0.

$$y = 175.75(0) + 903.75 = 903.75$$
 (about 904 people)

To get the population in 2014, plug in t = 14.

$$y = 175.75(14) + 903.75 = 3364.25$$
 (about 3364 people)